## THE UNITED REPUBLIC OF TANZANIA NATIONAL EXAMINATIONS COUNCIL ADVANCED CERTIFICATE OF SECONDARY EDUCATION EXAMINATION

142/1

## ADVANCED MATHEMATICS 1

(For Both School and Private Candidates)

Time: 3 Hours

Monday, 04th May 2015 a.m.

## Instructions

- 1. This paper consists of ten (10) questions, each carrying ten (10) marks.
- Answer all questions.
- 3. All work done in answering each question must be shown clearly.
- 4. Mathematical tables and non-programmable calculators may be used.
- 5. Cellular phones are not allowed in the examination room.
- 6. Write your Examination Number on every page of your answer booklet(s).

SV = OA + JAB



- Using a non-programmable calculator: 603
  - Calculate  $\log_{+}(e^{x} + 2\ln 5) + \log 5$  and write your answer to xix decimal places.
  - Obtain the value of  $\sqrt{\frac{(4.03)^3 \times (814765)^{6.5}}{\sqrt{5}}}$  to three significant figures. (iii)
  - Find the value of  $\left(\frac{{}^{6}C_{3} \times \ln 2}{4/43}\right) \times \begin{vmatrix} 3e & \ln 2 \\ e & \ln 2 \end{vmatrix}$  to four decimal places.
  - Evaluate  $\sum_{i=1}^{3} e^{i\alpha y} (1 + (y+1) \ln y)$  to four significant figures. (6)
  - Express  $4\cosh\theta + 5\sinh\theta$  in the form  $r\sinh(\theta + \alpha)$  giving the values of r and 03 (A) tunh cz
    - Prove that  $\cosh^{-1} x = \ln(x + \sqrt{x^2 1})$
    - Show that  $\frac{1}{2} \sinh(2\ln x) \cosh(2\ln x) = \frac{1}{8x^4} (x^2 1)$ . (b)
      - Find the possible values of  $\sinh x$  if  $\cosh x \sinh x = 2$ . (Leave your  $\sinh x + \cosh x = 2$ .) answer in surd form)
    - Sketch the graph of y = sinh 's and state its domain and range
    - A company owns two mines. Mine A produces 1 ton of high grade one, 3 tons of medium grade ore and 5 tons of low grade ore each day, and mine B produces 2 tons (2) of each of the three grades of ore each day. The company needs 80 tons of high grade ore, 160 tons of medium grade ore and 200 tons of low grade ore, How many days should each mine be operated if it costs she 200,000% per day to operate each mine?
      - A sugar company ships sugar from two origins S, and S, to three market centers Mo. M2 and M3. The table showing the available tons of sugar and the required tons together with the unit transportation cost in shillings is shown below

Mi	M <sub>2</sub>	Ma	Available
	10	5	220
		30	100
	_	The second second	
	M <sub>1</sub> 20 10 120	20 10 25	20 10 5 10 25 30

- Use the given information in the table to formulate the objective cost function
- Z to be minimized Write down all equalities and inequalities of the transportation problem.

- (iii) Verify whether the transportation problem in 3(b) is a balanced one or not. Use Xij's to denote the amount transported from source i to destination j.
- Kamimonge cooperative farm with 20 branches each recorded one among the following sales of wheat last month: 6.0, 100, 223, 343, 375, 343, 294, 100, 13.54, 32, 156, 276, 213, 20.5/313, 47.9, 46.3, 41.4 and 48.2. Group the data into class intervals 0 10, 10 20, etc. and determine:
  - (a) (i) Mode of the data correct to 4 significant figures.
    - (ii) Median of the data.
    - (iii) The standard deviation correct to 4 significant figures.
  - (b) The lower and upper quartiles.
- (a) (i) Use a Venn diagram to show that  $(A \cap B) \cup (A' \cap B) = B$ .
  - (ii) Find the members of set R where  $R = \left\{ x : \frac{x^2 9}{x^2 1} \le 0, x \in \mathbb{R} \right\}$
  - (b) Use the basic properties of set operations to simplify the following:
    - (i).  $(A \cap B) \cup (A B)$ .
    - (ii) [(ACB) n(AnB)].
  - (c) In a bunch of twenty flowers, twelve are yellow and nine are red. If four of the flowers are neither yellow nor red, how many of the flowers are both yellow and red? (Use Venn diagram).
- (a) If  $f: x \to 5x + 4$  and  $g: x \to 6x k$ 
  - (i) Determine the value of k for which  $f \circ g(x) \circ g \circ f(x)$ .
  - (ii) Prove that f + (f + f(x)) = 125x + 124
  - (b) Draw the graph of  $\frac{2x^3}{x^2-9}$
- (a) Starting with x<sub>e</sub> = -1, approximate the root of f(x) = x + e' in four iterations using
  the Newton-Raphson method. All your iterations should be presented in five
  significant figures.

- (b) (i) Apply both Simpson's and Trapezium rule with eleven ordinates to find an approximate value of ∫sin(1 + √x)dx. Give your answers correct to four decimal places.
  - (ii) Why does Simpson's rule said to be more efficient than trapezium?
- 8. (a) (i) Sketch the diagram of the locus of points which move such that they are equidistant from two intersecting lines.
  - (ii) Find the equations of bisectors to two intersecting lines whose equations are 6x 8y = -7 and 4x + 3y = 12.
  - (iii) Find the equation of the locus of points which is equidistant from the lines y = 2x and 2x + 4y 3 = 0.
  - (b) Determine the distance of the point (8, -6) from the line 2x + 5y + 34 = 0.
- 9. (a) Integrate \( \int \text{sec}^3 x \, dx
  - (b) Evaluate  $\int_{-1}^{0} \left( \frac{2x+3}{x^2+2x+4} \right)$
  - (c) Find the area of the region bounded by the graphs of  $y = \sin x$  and  $y = \cos x$  between x = 0 and  $x = \frac{\pi}{2}$  (leave your answer in surd form).
- 10. (a) If  $y = (1 + 2t)^3$  and  $x = t^3$ , find  $\frac{dy}{dx}$ 
  - (b) Find  $\frac{d}{dx} \left( \tan \sqrt{6x^3 + 2} \right)$
  - (c) (i) If  $U = x^3 e^x$ , find dU

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(ii) Show that  $(3x^2y - 2y^2)dx + (x^2 - 4xy + 6y^2)dy$  can be written as an exact differential equation of a function  $\phi(x, y)$  and find this function.

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