

THE UNITED REPUBLIC OF TANZANIA
NATIONAL EXAMINATIONS COUNCIL
ADVANCED CERTIFICATE OF SECONDARY EDUCATION
EXAMINATION

141

BASIC APPLIED MATHEMATICS
(For Both School and Private Candidates)

Time: 3 Hours

Monday, 11th February 2013 a.m.

Instructions

1. This paper consists of **ten (10) compulsory** questions. Each question carries **ten (10)** marks.
2. All work done in answering each question must be shown clearly.
3. Mathematical tables and non programmable calculators may be used.
4. Cellular phones are **not** allowed in the examination room.
5. Write your **Examination Number** on every page of your answer booklet(s).



1. By using a non programmable calculator:

- (a) Compute the value of $\sqrt[3]{\frac{3,141 \times 2,751}{47 \times 39,8}}$ and write your answer in 6 decimal places.
- (b) Find the sum of the finite series $2\left[\frac{1}{1 \cdot 2^1} + \frac{1}{3 \cdot 2^3} + \frac{1}{5 \cdot 2^5} + \frac{1}{7 \cdot 2^7} + \frac{1}{9 \cdot 2^9}\right]$ and write your answer in 4 decimal places.
- (c) Find the mean length of 200 engine components that were measured and recorded as follows:

Length (mm)	198	199	200	201	202
Frequency	8	30	132	24	6

- (d) Find the value of ${}^{15}P_6 \times {}^{10}P_2$.
- (e) Compute the value of ${}^8C_5 \times {}^{11}C_2 \times 9!$

2. (a) The functions f and g are defined by $f: x \mapsto \ln x$ and $g: x \mapsto e^x$.
- (i) Sketch the graphs of f on $0 \leq x \leq 3$ and g on $-3 \leq x \leq 3$ on the same x and y plane.
- (ii) State the domain and range of f and g .
- (iii) Identify the asymptotes for f , g and describe briefly how f and g behave near the asymptotes.

(b) Given $f(a) = \frac{a-1}{a+1}$, show that $f\left(\frac{1}{a}\right) = -f(a)$.

3. (a) The first four terms of the series A, B and C are given below. Among the series, one is an arithmetic series, one is a geometric series and the remaining is neither.

(i) A: $128 + 64 + 32 + 16 + \dots$

B: $4 + 8 + 12 + 24 \dots$

C: $38 + 35 + 32 + 29 + \dots$

- (i) State the value of the common difference of the arithmetic series and calculate the 21st term of this series.
- (ii) Find S_{10} of the geometric series.

- (b) If the length of a paper in a roll of given dimensions varies inversely as the thickness of the paper, find the increase in length when the thickness of a paper in a 100 m roll is decreased from 0.25 mm to 0.20 mm.

4. (a) Differentiate with respect to x the functions:

(i) $f(x) = e^{\sin x}$,

(ii) $y = \frac{3}{x^3} - \frac{1}{\sqrt{x}}$,

(iii) $x^2 + xy + y^3 - 2x + 3y = 0$.

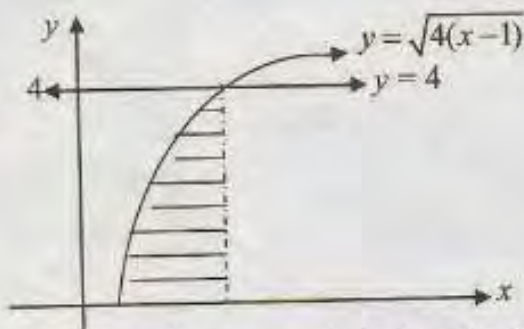
(b) Find the turning points of the polynomial function $y = x^3 - x^2$ and hence sketch the graph of this function.

5. (a) Evaluate the integrals:

(i) $\int \sin(4x + 6) dx,$

(ii) $\int_0^1 (x^3 + 1)^2 dx.$

(b) The graph of $y = \sqrt{4(x-1)}$ is shown in the sketch below together with the line $y = 4$.



Find the volume generated when the shaded area is rotated completely about the x-axis, leaving your answer in terms of π .

6. The scores of 40 students in a mathematics test are given below.

Scores	21 - 30	31 - 40	41 - 50	51 - 60	61 - 70	71 - 80	81 - 90
Number of students	3	6	10	8	6	4	3

(a) Represent the students' scores in a histogram and then use it to calculate the mode.

(b) Find:

- (i) Variance of the scores,
 (ii) The standard deviation of the scores.

7. (a) (i) Draw 2 possible venn diagrams representing two events A and B in a sample space S and then write down the formulae corresponding to $P(A \cup B)$.

(ii) Given that A and B are mutually exclusive events with probabilities

$$P(A) = \frac{1}{4} \text{ and } P(B) = \frac{2}{3}, \text{ find } P(A \cup B)'.$$

(b) Ntibagomba is going on holiday. He has 6 different shirts and has decided that he only needs to take 3 shirts. Find the number of different selections that he can make.

(c) Find the number of ways that six children Kauki, John, Tito, Ben, Kato and Sara can stand in a line outside the canteen waiting for lunch.

8. (a) If A is an acute angle such that $\tan A = \frac{3}{4}$, find without using tables or calculator, the values of (i) $\cos 2A$ and (ii) $\sin \frac{A}{2}$.
- (b) Solve the equation $2\sin(x + 60^\circ) = \cos(x - 30^\circ)$ in the range $0^\circ \leq x \leq 360^\circ$ by expanding the sine and the cosine terms.

9. (a) Given that $A = \begin{pmatrix} 3 & 1 \\ 5 & 2 \end{pmatrix}$ and $B = \begin{pmatrix} -4 & 3 \\ -5 & 2 \end{pmatrix}$, verify that $(AB)^T = B^T A^T$.

- (b) Show whether the following system of equations has a common solution or not.

$$7x - 3y - 3z = 7$$

$$2x + 4y + z = 0$$

$$-2y - z = 2$$

- (c) The results of three soccer teams Simba (S), Yanga (Y) and Mtibwa Sugar (M) are shown in matrix R and the points awarded for each team in matrix P.

$$R = \begin{matrix} & \begin{matrix} W & D & L \end{matrix} \\ \begin{matrix} S \\ Y \\ M \end{matrix} & \begin{pmatrix} 6 & 2 & 4 \\ 4 & 3 & 1 \\ 7 & 1 & 4 \end{pmatrix} \end{matrix} \quad \begin{matrix} \text{Points} \\ W \\ D \\ L \end{matrix} = \begin{pmatrix} 5 \\ 1 \\ 0 \end{pmatrix}$$

Multiply the matrices and hence state which team has many points.

10. The data for M & P Company, which manufactures tables and chairs, is given in the table below:

	Labour Hours per Item		Maximum Labour Hours Available
	Table	Chair	
Assembly Department	16	4	800
Finishing Department	4	2	240
Profit per Item	Shs. 10,000/=	Shs. 4000/=	

- (a) How many tables and chairs that should be manufactured to realize a maximum profit?
- (b) What is the maximum profit?